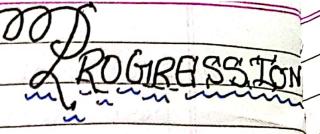
RITHMETIG



Sequence :- An arrangement of numbers in an definite aroler or \$10 specific pattern forms a sequence.

For e.g.

(1) 2,4,6,8,10,---
(2) 3,6,12,24,48,---
(3) 1,4,9,16,25,----

In general the nm term of a sequence 18 denoted by Zan> or {and}

Types of Sequences

There are three types of sequences

- (2) Arstmetic Progression (A.P.)
- 3) Gieometere Progression (GI.P.)
- (3) Harmonde Progression (H.P.)

1) Austhmethe Progression & Fin austimeter preogression is a clost of numbers in which each term is oblighted by adding, a fried number to the preceding, term except the frest term. This fixed number is called common différence of the A.P. Remember that it can be positive, negative or jero. Each mo. which forems an A.P. 98 called Levem of an A.P. Example 8-1 1,2,8,4,5, 200-1-06 100,70,40,10,4---(8) 3,3,3,3,3,----NOTE & The frest terem of an A.P. 88 denoted ley "a" & common difference & denoted ley "d".

Hest teem = q Common difference -d into teem gren authmotte progression. n m terom = a + (n-1) d Second Team - Hest revom = Third Team - Sectional Team = 4th Team - 3th Team
(4+24) (4+4) (4+4) (4+4) (4+4) 30 Js an AD Sum of n terems 8 Sn = n/2 [frest telem + 'clast toum] Sn= m/2 & 2a+ (n-1) d}

a = -2, d = 0We know that, hard would be Q2 = -2 +0 = -2 03=+2+2(0)=-2 94=-2+3(0)=-2 00 Hest force terms are -2, -2, -2, -2 We know that, a = as , = 1411 wond du -- (d₃ = 4+2(-3) = -2 3 99 = 9 + 3 (-3) = -5 3 = Frest four terms are 4, 1, -2, -5

when of the following AP's & If they form an AP, find the common difference of and coulte twee more terms 2,4,8,16 First term, a = 2common difference, d = 92 - 91 = 4-2== common difference is not same or equal.

-10, -6, -2, 2Frest term a = -10 = 4 = 4 3. St & an AP. so Next-twee terms are; = -10+4(4) = -10 + 16 = 6a6 = a+5b =-10+6(4)-10+20=10Mext when it a7 = a+6b1 =-10+6(4)=-10+24=14

CXII	7) V3, V6, V9, V12,
	$\Rightarrow a = \sqrt{3}$
	$d = \sqrt{6} + \sqrt{3}$
	$= \sqrt{3} \times \sqrt{2} - \sqrt{3}$
	$=\sqrt{5}(\sqrt{2}-1)$ $\sqrt{3}(\sqrt{2}-1)$
	= 93 - 92
	$ =\sqrt{9}-\sqrt{6}$
	$= \sqrt{3} \times \sqrt{3} = \sqrt{3} \times \sqrt{2}$
	= 3-VE V3 (V3-VE)
	30 It 98 not an AP.

The amount of are present in a cylinder when a vaccuer pump removes 1/4 of the are remaining in cylinder at a sing Let amount of ale present in a cylinder of Ame t le gre. After veemoving 1/4 of the axis from cylinder, it will veemoun 1/4 of the axis from 1/4 -1 /2 - 3 n Heer removing 1/4 of the 32/4

Shifted semoving 1/4 of 32/16 of ale from cycloder, it remains

9x - 9x = 27x

16 64 64

co It is not an AP as its common difference is not similar.

The amount of money in the account every year, when \$ 10,000 is deposited a compound interest at 8% per amum. Amount for 1t years PS, 10000 10000 10800 10800 80 10000 Z800

Amount for 2nd year, $A = P \left(1 + 8 \right)^{2}$ A - 10000 X 108 X 108 Amount for 3rd year, $A = 10000 \left(\frac{1}{100} \right)^3$ A = 108 × 108 × 108 100 108 x 781664 CLICK HERE (>> Get More Learning Materials Here: www.studentbro.in

= 12597 (00 A = 125.97 2s St 18 not an AP MITH TERM OF AN AP If 'g' 38 the frest term & "d' 38 common difference of an AP then the min term of an AP & given by an = a + (n-1) d 3 > + sruomf cohece, n = no. of terms teleme of an AP & also denoted by it

(9)	d=7, d=3, m=8, an=2
	2-5 1- 12-21- 1- 12-21- 1- 12-21- 1- 12-21- 1- 12-21- 1- 12-21- 1
->	$a_n = g + (n-1)d$
	98=7+(8-1)(3/2000)
	08 = 7+212 = 28 m) 18-31
	7-5(I-N) FOB. 30+3.6
(۱۱)	a = -18, d = ? , m = 10, an = 0
	T-16 = 2 = 7 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 -
->	an = a +(n-1) d
	90 = -18 + 9d
	18 = 90
	2 d = 2 701 = 17 0 = 10 1 1 3 = 18 (b)

<u>П</u>, 13, П, 3 q = 8, $q_2 = 13$, $q_3 = 8$, $q_4 = 3$ az = a+d=13 d+3d=3 subteact D&D 0 + 0 = 130 m _d+3d=3 -2d = 1g d= -5 From eq. D 9-5=13 9 = 18 03 20 + 20 = 18+2(-5) = 18 - 10 = 8 80 AP 694 lee 18, 13, 8,3.

Check whether -180 98 a seem in each of the following AP = 11 , 8,5,2 DAO NENDE 9-11 30m = -150 en bolt an = a + (n-1)d 0 -150 = 11 + (n-1)(-3)+ 161 = m-1008 + D = 100 161 SOL STANDARD LOUIS BELL TO SOL 8. It 98 not a term involve in AP as Mzn term commot be in fraction.

Find the 31st teem of om AP whose 11th tem and 16th teem 8 78. R 38 911 = 38 a16 = 73 an a + 10d = 38.91 d + 15d = 73Subtract D & D LE = B a + 70 = 38 9 + 100 = 381d = 38-70-d + 15d = 73 a = -32-5d = -35 15-)(I-40) + II - 02 F = 01 + 300931 = -32 + 30(7)=-32+210

Ramkall Saved 25 In the frest week of a year and then Increase her weekly lawing leep 21.75. If In thenth weekly her weekly savings become 220.75, According to given corolition a = 5, d = 1.75, m = 2, an = 20.75an = a + (n-1) d 20.75 = 5 + (m-1) 1.7515.75 = (n-1) 1.75n = 1080 7210

Sum of Frest on Terems of an AP If 60' & 6d' are frest terem & common defference of an AP then the sum of thest n terms of an AP 38 denoted by Sn & 98 given by $S_{n} = n \left[2q + (n-1)d \right]$ It is is the frest term & in some som of them seems of given by Sn=n (a+l)

Isnd the sum of fallowing AP 3: 2, 7, 12, ---, to 40 teams Here, d=2, d=5, m=10 coe lenow, $S_n = m [2a + (n-1)d]$ S10 = 5 [4+45] 510 = 15 X49 10 S10 = 245 o's Sum of ten derems is 245.

7+10101 +19, ---, +84 $\frac{77\times2}{7}=(n-1)$

(N) gren 93 = 15, S10 = 125, Find d 4 920 $S_{n} = \frac{n}{3} \left[2a + (n-1)d \right]$ S10= 10 [2(15-2d)+9d] 6 (1-m) + 0 = 40 325 = 5 [30-40+9d] 0= / (II) + D = TE \$25 = 3045d CE D 52 5d d = -1 Fotol G d = 15 - 2d. q = 15 - (2)(-1) + 1a = 15 + 2 a = 17To so of an = af (m-1) d a10 = 17 + (10 -1) (-1) $Q_{10} = 17 + (9)(-1)$ $q_{10} = 17 - 9$ 910 = 8 Get More Learning Materials Here: CLICK HERE (>>)

(VP)	gren a = 2, d=8, Sn = 90, and n anda,
	TON- DE J. DE SY
>	$S_n = n [2q + (m-1)d]$
	2 miles and and a second and a
	# 150 - 19 - 102t
indi den pila seja maga	$90 = n \left[4 + (n-1)8\right]$
And the second	038 + 1081
All of Control of Control	$90 = m \left[4 + 8m - 8 \right]$
Chillippin recently	5 OV - OLL O O
Control of Control	

180 = m [4+8m-8] $180 = 4n + 8n^2 - 8n$ $180 = 8n^2 - 4n$ an - 180 = 0 4(2n2-14) =180 $2n^2 - 24 = 45$ $2n^2 - n - 45 = 0$ 2n2+9n-10n-45=0 n (2n+9)-5(2n+9)=0 (2n+9)(n-5)=0@ 2n+9=0 6 m-5=0 n=-9/2 & n=5 30 n connot be in franction 30 n =5 an = a + (n-1) d as = 2 + (8-1)8 95 = 2+(4)8

95 = 2 + 32

95 = 34

Ind the sum of frest 51 derms of an AP whose second and thread terms are 14 and 13 respectively. a2 =14 013 =18 d = 93-92 = 18+19=9+ a2 = a+d 14 = 9 + 4 La=10 Sn=n [2a+(n-1)d] $S_{51} = 51$ [2×10+(51-1)×4] $= 51 \left[2 + (20) \times 4 \right]$ 51 × 110 5610

If the sum of frest n terms of an AP & $4n-n^2$, what is the sum of if est the series? What is the second terms? Simplicatly find the thed the 10th and the nth terms?

Given $Sn = 4n-n^2$ $a = S_1 = 4(1)-(1)^2 = 4-1=3$

[an = Sn - Sn-1] $\frac{2um}{3um} = \frac{6}{3um} + \frac{$ $d = a_2 - a_1 = 1 - 3 = -2$ an = a+(n+1)d1 n)11 =3+(m-1)(-2)= 3-1271 +210 + 3×5 1 04 = 5-22 8, 93 = 5 - 2×3 = 5-67-1 00 = 10 a10 = 5 -2 ×10 = 5 + 20 = -15 3 2 X 0 2 = 1.6 Hence, sum of frest two terms 884. Second terms 8 1- 3rd, 10th, and nth terms are 1,-15 6 5-2n respectively